## **10th Annual Cubesat Developer's Workshop**

# Design optimization of a Solar Panel Angle and its Application to CubeSat 'CADRE'

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Goal : To develop a process that determines static solar panel angles for optimal power generation

[1]"Analysis of Solar Panel Orientation in Low Altitude Satellites" IEEE Transactions on Aerospace and Electronic Systems VOL. 34, NO. 2 APRIL 1998

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## Introduction

- Many CubeSats are power constrained.
  - There is not enough space for the solar cell installation.
  - Low Earth Orbits have varying eclipse times.
  - **Existing solutions** 
    - **Deployable panels : ex. 'Space-dart' configuration**
- Question : How can we maximize the utility of deployable panels?
  - What is the best pointing angle for the panels?
    - Anigstein et al<sup>[1]</sup>. developed a optimal pointing angle decision methodology. •
    - But they assumed no shadow on panels. •
  - How do you assess the impact of solar panel shadow?
    - Consideration of the shadow effect is important during the satellite design.
    - More deployable panel can cast more shadows.



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## **Objective Function Candidates**

• Problem : What is the best panel angle in the given orbit parameter



• There are multiple objective functions for the power generation optimization

 $\max\left\{\int_{0}^{T} P(x, O_{p}, t) dt, T = 1 \text{ year}\right\}$  - Maximization of the total power generated during 1 year period

$$\max\left\{\min\left\{\frac{1}{T}\int_{(n-1)T}^{nT}P(x,O_p,t)dt, \ T=1 \text{ orbit}, \ n\in\left[0 \quad \frac{1 \text{ year}}{T}\right]\right\}\right\} - \text{Maximization of the minimum orbit} \\ \text{average power which was recorded} \\ \text{during 1 year simulation period}$$

 $\max\left\{\min\left\{P(x, O_p, t), t \in [0, T_{orbit}]\right\}\right\} \quad \text{-Maximization of the low limit power generated during 1 orbit period (Sun synchronous Orbit)}$ 





## **Simulation Process**

• Simulation Process for the power evaluation





• Sun position mapping in the attitude sphere<sup>[2]</sup> can be done based on the simulation



[2] J.C. Springmann and J.W. Cutler "Optimization of Directional Sensor Orientation with Application to Photodiodes for Spacecraft Attitude Determination", Proceedings of the 23rd AAS/AIAA Spaceflight Mechanics Meeting, Kauai, Hawaii, February 2013.

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• We calculate the solar cell surface area projected in the direction of the Sun

- Using OpenGL , we calculate the area quickly and make a database .

Panel angle : 20° / Panel name : +b / Cell number : 7



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• Sum of each cell's projected area in the attitude sphere



• We use a following equation to calculate the generated power by solar cells

$$P(x, O_p, t) = S_0 \cdot \varepsilon \cdot \sum_{i=1}^{12} \sum_{j=1}^{7} A_{i,j} \left( x, \varphi_{sun}(O_p, t), \theta_{sun}(O_p, t) \right)$$
$$= S_0 \cdot \varepsilon \cdot A_{Total} \left( x, \varphi_{sun}(O_p, t), \theta_{sun}(O_p, t) \right)$$
$$S_0 \approx 1366 \text{W/m}^2, \ \varepsilon \approx 28\% \qquad 0^\circ \le x \le 90^\circ, \ 0^\circ \le \varphi_{sun}(O_p, t) < 360^\circ, \ 0^\circ \le \theta_{sun}(O_p, t) \le 180^\circ$$

 It is assumed that solar power generation is proportional to the solar cell surface area projected in the direction of the Sun.





#### • Panel angle value can be found out by exhaustive search on design space



• In this exhaustive searching process, the range of the panel angle x is 0°, 3°, 6°, ..., 90°



- the major parameters which affect solar power generation are the inclination(*i*) and RAAN( $\Omega$ )
  - Because, the Sun incident angle to orbital plane is decided by the inclination(*i*) and RAAN( $\Omega$ )
- The calculation speed is accelerated with MATLAB/Simulink coder and OpenGL
  - Area calculation with OpenGL: 1 DB generation takes about 4 min.
  - 1 year simulation with 10 second time interval takes about 5 min





### Panel angle optimization of the Sun-synchronous orbit





## Panel angle optimization of the Non Sun-synchronous orbit

- Panel angle :  $0^{\circ} \sim 90^{\circ}$
- Inclination : 0  $^{\circ} \sim 82^{\circ}$
- In the given inclination range, the moving speed of RAAN(Ω) is greater than 360°/1year
  - Then we can rule out the RAAN( $\Omega$ ) effect and compare the inclination and the panel angle's relation.







## **Result Analysis of Non Sun-Synchronous orbit** (Inclination : 67°)

- Small panel angle has smaller daily deviation of the power than the large panel angle
- However, Large panel angle has smaller yearly deviation of the orbit average power than small panel angle





### Result Analysis of Sun-Synchronous orbit ('Noon-Midnight' Orbit)

- Altitude : 700km , Inclination : 98°, Launching date : 3-20-2015
- During 1 year, the orbit average power has no change.









- Altitude : 700km, Inclination : 98°, Launching date : 6-20-2015
- If altitude is  $\geq$  1,060km, the eclipse period will not appear.



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# Conclusions

- Advanced panel angle design optimization technique
  - Based on the result of the numerical simulation of every possible condition
  - Shadow effects consider
    - Deployable panels to other deployable panels
    - Deployable panels to the body panels
  - Dynamics consider
    - Orbit dynamics with J2, J3, J4.
    - Attitude dynamics
- Future work : EPS design optimization
  - Solar cell IV curve characteristic Modeling
  - Cell/Radiator thermal characteristics.
  - Battery characteristic
  - Albedo consideration
- Large scale Multidisciplinary Design Optimization(MDO) of Cubesat
  - Because the running all possible case simulation is very exhaustive and not practical
  - Researching 'Gradient based optimization'





# Large Scale Cubesat MDO

